

Credit Risk

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BUSI 448: Investments

Where are we?

Last time:

- More interest rate risk
- Convexity
- Callable bonds

Today:

- Credit risk
- Credit ratings

Credit risk

Credit risk: the risk that the issuer of a bond (borrower) will not pay back all or part of the promised cash flows.

Issuers with credit risk:

- Corporations
- Households
- Governments

Credit ratings

Investment-grade versus high-yield

	Moody's	S&P + Fitch
Investment Grade	<ul style="list-style-type: none">• Aaa• Aa• A• Baa	<ul style="list-style-type: none">• AAA• AA• A• BBB
High-Yield (Junk)	<ul style="list-style-type: none">• Ba• B• \leq Caa	<ul style="list-style-type: none">• BB• B• \leq CCC

- Higher ratings generally mean less default risk.
- There are + and - notches for the ratings above.

Purposes of ratings

- Proxy for credit risk
- Regulation
 - Ex: Capital req's are often tied to ratings
- Contracting
 - Downgrades may trigger contract clauses

Modeling corporate credit

Modeling corporate credit

- Why would a 5-year IBM bond have a different yield from a 5-year AAPL bond?
 - industry differences
 - firm-specific information
 - capital structure

Let's take a look at some data.

Regression analysis #1

$$y_{it} = \beta_0 + \beta_1 \cdot \text{ttm}_{it} + \beta_2 \cdot \text{rating}_{it} + \varepsilon_{it}$$

- rating is numeric 1, 2, 3, ...
 - we might want to do this differently

Average yield by ratings class

- Let's calculate the average yield within each ratings class.
- What should we expect to see as credit ratings decline?

Code to average by ratings class:

```
1 df.groupby('RATING_CAT')['ytm'].aggregate(['mean', 'count'])
```

Regression analysis #2

- It's possible that yield-ratings relation will be non-linear.
- One way to capture this is to add dummy variables for each ratings bin:

$$y_{it} = \beta_0 + \beta_1 \cdot \text{ttm}_{it} + \sum_{k=AA,A,\dots} \beta_k \cdot \mathbf{1}[\text{rating}_{it} = k] + \varepsilon_{it}$$

Code to generate dummy variables:

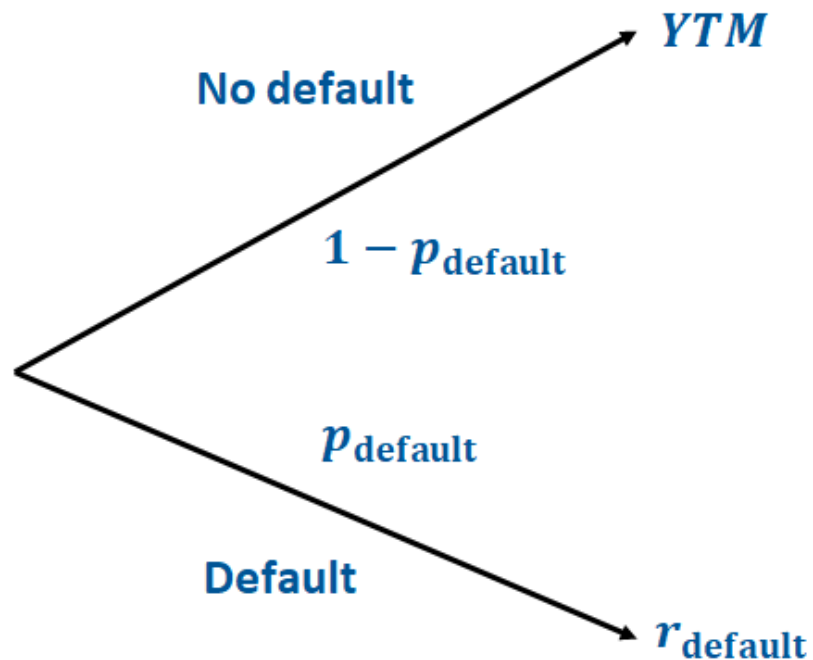
```
1 rating_dummies = pd.get_dummies(df.RATING_CAT)
2 df = df.merge(rating_dummies, left_index=True, right_index=True)
```

Regression versus within-class averages

- How do the within-class averages compare to the dummy-variable regressions?
- NOTE: this would be *exact* if we hadn't controlled for time-to-maturity.

For a risky bond, $YTM \neq$ expected return!

- YTM: IRR of a bond based on **promised** cash flows.



$$E[r] = (1 - p_{\text{default}}) \cdot YTM + p_{\text{default}} \cdot r_{\text{default}}$$

YTM overestimates expected returns for risky bonds.

Credit Spreads

Yield Spreads

- Bonds with credit risk are often quoted as an interest rate spread relative to some benchmark rate
 - Treasury of same maturity or a interest rate swap

$$\text{Spread} = YTM_{\text{risky}} - YTM_{\text{maturity-matched risk-free}}$$

- Spread is related to the default probability times the expected loss given default (in risk-neutral terms).
 - \uparrow in probability of default increases spread
 - \uparrow in expected loss given default increases spread



Credit spreads

More Fixed Income

CDS

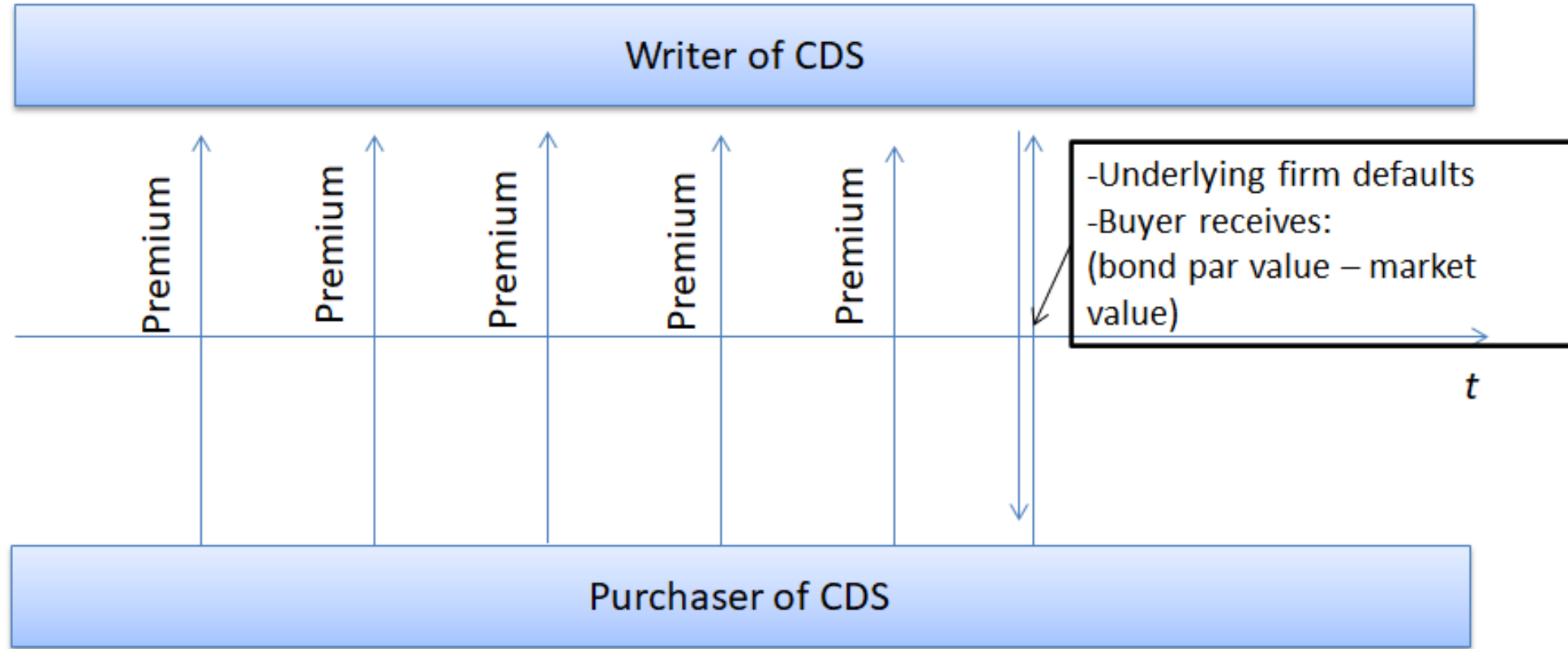
Credit default swaps

Credit default swaps: an insurance contract against default by a risky borrower

Two cash flow streams:

1. CDS buyer pays CDS seller a period payment (**premium**)
 2. If firm defaults, the CDS seller pays the buyer the bond's par value less the bond's market value.
- CDS contracts are intended to make an investor in an issuer's debt whole in the case of default.

CDS cash flows



No-arbitrage relation

- There is a no-arbitrage relation between a corporate bond, risk-free debt, and a CDS.
- The cash flows from owning a risky bond + CDS should be the same as owning a risk-free bond.
- The **Law of One Price** says that two portfolios that generate the same cash flows in the future should have the same price today!
 - This implies that:

$$\text{Bond Yield Spread} = \text{CDS spread}$$

Cash flows with and without default

Let $R < 100$ denote the recovery for a defaulted bond.

With default, the payoffs are:

Risky Bond	Risk-free Bond	CDS
R	100	100-R

With no default, the payoffs are:

Risky Bond	Risk-free Bond	CDS
100	100	0

- Risky Bond + CDS provides \$100 either way!

Uses of CDS

- Hedging of credit risk by long bond investors
- Speculation
 - buy CDS if you think an issuer will default
 - sell CDS to collect premiums

Economic debates

- *Empty creditor problem:*
 - is it good for bondholders to *not* have exposure to firm's credit risk?
 - will these investors monitor effectively?
- *Counterparty risk:*
 - CDS writers could be on the hook for a large amount in the event an issuer defaults. Will they be good for it?
- *Legal questions:*
 - What constitutes a default?

For next time: Asset Management

